

# Endmember-Aware Feature Learning for Nonlinear Hyperspectral Unmixing

Suraj Tripathi

Department of Computer Science, Binghamton University, Binghamton, NY, USA.  
surajtripathi760@binghamton.edu

Uday Tripathi

Department of Computer Science and Engineering, University of Nevada, Reno, Reno, NV,  
USA.  
tripathi341@unr.edu

Warren Burns

Department of Computer Science and Engineering, University at Buffalo, Buffalo, NY, USA.  
warrenwork@buffalo.edu

Ruben Walters

School of Computing, Clemson University, Clemson, SC, USA.  
walters274@clemson.edu

## Abstract

Hyperspectral unmixing is a critical inverse problem in remote sensing that involves decomposing mixed pixels into a set of pure spectral signatures, known as endmembers, and their corresponding fractional abundances. Traditional unmixing approaches often assume a linear mixing model, but many real-world scenarios exhibit nonlinear interactions due to multiple scattering, intimate mixing, and complex surface geometries. This paper presents a comprehensive system-level analysis of endmember-aware feature learning frameworks designed to address the challenges of nonlinear hyperspectral unmixing. We argue that embedding endmember knowledge directly into the feature learning process enhances both interpretability and accuracy, while also introducing structural trade-offs that affect deployment, scalability, and governance. The discussion spans architectural design choices—such as the integration of spectral-spatial constraints, attention mechanisms, and state-space models—and examines how these choices influence robustness under varying illumination, atmospheric conditions, and sensor noise. Sustainability considerations are explored in terms of computational resource demands, energy efficiency, and model longevity across diverse observational platforms. Furthermore, we address fairness and policy implications, including the risk of spectral biases introduced by training data imbalances and the need for transparent unmixing pipelines in environmental monitoring and resource management. By synthesizing recent advances in deep learning with domain-specific constraints, we outline a forward-looking perspective on infrastructure governance and the responsible deployment of unmixing systems. The paper concludes with recommendations for future research directions that prioritize algorithmic transparency, cross-domain generalizability, and equitable access to high-quality Earth observation data.

## Keywords

hyperspectral unmixing, nonlinear mixing, endmember-aware learning, deep neural networks, remote sensing, spectral variability, system robustness, fairness, environmental policy, infrastructure governance.

## 1. Introduction

Hyperspectral imaging captures reflectance information across hundreds of narrow contiguous spectral bands, enabling detailed discrimination of materials on the Earth's surface. However, the spatial resolution of hyperspectral sensors is often limited, causing each pixel to record a mixture of spectral contributions from multiple materials. Unmixing serves as a fundamental preprocessing step that recovers the pure spectral signatures (endmembers) and their proportional abundances from such mixed observations [1], [2]. While many operational systems adopt linear mixing models due to their mathematical tractability, the assumption of linearity breaks down under conditions where photons interact with multiple materials before reaching the sensor, a phenomenon known as nonlinear mixing [3]. These nonlinearities are particularly pronounced in vegetated areas, urban canopies, and scenarios involving intimate mineral mixtures.

Recent advances in deep learning have opened new pathways for modeling nonlinear mixing processes. Among these, endmember-aware feature learning has emerged as a paradigm that explicitly incorporates knowledge about endmembers into the representation learning pipeline, rather than treating them as latent variables to be inferred in a separate step [4], [5]. This approach promises to improve unmixing fidelity while also providing interpretable intermediate representations. Nevertheless, transitioning from a linear to a nonlinear endmember-aware framework introduces significant system-level trade-offs that span algorithmic design, computational infrastructure, and broader societal implications. The present paper examines these trade-offs from an interdisciplinary perspective, drawing on insights from systems engineering, artificial intelligence governance, and environmental policy. We aim to provide a holistic understanding of how endmember-aware feature learning can be robustly deployed at scale, what sustainability challenges it poses, and how fairness concerns arise in the context of global Earth observation data.

## 2. Background and System Context

Hyperspectral unmixing has historically been approached through geometrical, statistical, and sparse regression methods [1], [2]. Geometrical algorithms such as vertex component analysis and N-FINDR identify endmembers by searching for extreme points in the spectral feature space under the assumption that pure pixels exist [11], [12]. These methods are computationally efficient but fragile in the presence of noise and spectral variability. Statistical approaches model the mixing process using probabilistic frameworks, often incorporating spatial priors to regularize the solution [7]. However, they typically rely on linear mixing assumptions and can become intractable for high-dimensional data.

The advent of deep learning has shifted the focus toward learning nonlinear mappings directly from mixed spectra to endmembers and abundances. Convolutional neural networks, autoencoders, and attention-based architectures have been applied to unmixing tasks with promising results [5], [6], [19], [20]. Yet many of these models remain black boxes, offering limited insight into how endmember information is encoded. Endmember-aware feature learning attempts to bridge this gap by designing networks that explicitly represent endmember spectra as learnable parameters or as outputs of dedicated branches, thereby linking the feature learning process to physical material properties [4], [17].

From a systems perspective, the deployment of such models must account for the operational context of hyperspectral sensors. These sensors are often mounted on satellites, aircraft, or unmanned aerial vehicles, each with different constraints on data volume, transmission bandwidth, and on-board processing capability. The nonlinearities inherent in real-world scenes further complicate the calibration and validation of unmixing algorithms. For instance, atmospheric correction and topographic normalization introduce additional sources of uncertainty that interact with the mixing model [8]. Therefore, endmember-aware systems must be designed to tolerate these perturbations while maintaining interpretable outputs. The following sections dissect the architectural choices, trade-offs, and governance implications of this emerging class of unmixing frameworks.

### **3. Architectural Considerations for Endmember-Aware Learning**

The core architectural innovation in endmember-aware feature learning lies in the explicit integration of endmember representations within the network. Rather than learning a latent space that indirectly encodes spectral signatures, these models often include a dedicated module that estimates endmembers from the input data, sometimes with spatial consistency constraints enforced through convolutional layers or graph-based regularization [5], [19]. The abundance estimation branch then leverages both the learned features and the estimated endmembers to reconstruct the mixed pixel. This structure creates a tight coupling between the two subproblems, which can improve convergence and reduce spectral confusion, but also introduces vulnerabilities when endmember estimates are noisy.

One prominent architectural trend is the use of attention mechanisms to highlight spectral bands or spatial regions that are most informative for distinguishing endmembers. Weak-signal attention fusion, as proposed in recent work, focuses on low-amplitude spectral features that are often masked by dominant materials [17]. Such mechanisms enhance sensitivity to subtle material variations but increase network complexity and require careful regularization to prevent overfitting to training-specific noise. Another design dimension is the incorporation of state-space models that capture temporal dependencies in time-series hyperspectral data, enabling dynamic unmixing for monitoring applications [17]. While state-space representations offer a principled way to model evolving mixtures, they demand sequential data and can be computationally expensive for large-area coverage.

Spectral-spatial hybrid architectures have also gained traction. By jointly processing the spectral dimension and local spatial neighborhoods, these networks can exploit contextual constraints—such as the smoothness of abundance maps—without resorting to explicit regularization penalties [6], [20]. However, the optimal balance between spectral depth and spatial receptive field is highly scene-dependent, and a fixed architecture may perform poorly across different landscapes. Endmember-aware designs thus require flexible tuning mechanisms or meta-learning strategies to adapt to varying geographic and climatic conditions. This architectural heterogeneity poses challenges for standardization and reproducibility across deployments, a point that has direct implications for infrastructure governance.

### **4. Trade-offs in Nonlinear Unmixing Systems**

Every architectural decision in an endmember-aware unmixing system involves trade-offs between accuracy, computational cost, interpretability, and generalization. Nonlinear models generally achieve lower reconstruction error on mixed pixels compared to linear baselines, yet this increased expressiveness comes at the risk of overfitting to spurious correlations present

in training data [3], [16]. For instance, a deep network trained on a particular sensor’s spectral resolution may fail to generalize to data from a different sensor with different band configurations or signal-to-noise characteristics. The endmember-aware constraint can mitigate this risk by anchoring the learned features to physically meaningful signatures, but the degree of anchoring must be carefully controlled: too strong a constraint may prevent the network from capturing nonlinear interactions, while too weak a constraint yields little benefit over purely data-driven approaches.

Another critical trade-off involves the handling of spectral variability. Endmember spectra are not static; they vary with illumination angle, atmospheric conditions, and material degradation over time [2]. Most traditional unmixing algorithms treat endmembers as fixed across the entire image, but endmember-aware feature learning can be extended to allow endmember adaptation on a per-pixel or per-patch basis. This flexibility improves local accuracy but dramatically increases the parameter count and the risk of ill-posed solutions. Moreover, adaptive endmember estimation introduces a coupling between abundance and endmember estimation that can lead to degenerate solutions where the network learns to produce arbitrarily large abundances for arbitrarily scaled endmembers. Regularization strategies, such as sparse coding or sum-to-one constraints on abundances, are essential but often conflict with the nonlinear nature of the mixing model [5], [6].

Scalability is a further concern. Hyperspectral images can be gigabytes in size, and real-time or near-real-time unmixing is required for applications such as disaster response or tactical surveillance. Deep learning models with attention mechanisms and state-space layers are computationally intensive, particularly during training on large datasets. Endmember-aware architectures that require iterative refinement or probabilistic inference exacerbate this burden. Deploying such models on edge devices—like small satellites or drones—necessitates model compression techniques, such as quantization, pruning, or knowledge distillation, which may degrade the endmember representation fidelity. The trade-off between inference speed and unmixing accuracy is therefore a central consideration for operational systems.

## **5. Robustness and Sustainability**

Robustness in hyperspectral unmixing pertains to the ability of a model to maintain acceptable performance under perturbations that are common in operational settings. These perturbations include sensor noise, atmospheric haze, misregistration between spectral bands, and variations in spectral resolution across different instruments. Endmember-aware feature learning must be designed with explicit robustness mechanisms, as the explicit representation of endmembers creates a direct pathway for errors to propagate from the feature extraction stage to the abundance reconstruction stage. For instance, if the endmember estimator is sensitive to additive Gaussian noise, the resulting abundance maps will reflect not only the material distribution but also noise artifacts [8], [9].

Data augmentation techniques, such as adding simulated noise or applying spectral transformations, can help improve robustness, but they increase the complexity of the training pipeline and may introduce unrealistic spectral patterns that degrade generalization. Adversarial training, where the network is exposed to worst-case perturbations, has been explored in other remote sensing domains but is still nascent in unmixing [4]. The integration of weak-signal attention, as investigated in recent work, can improve robustness to low-energy features that are often corrupted by noise, but the attention gating function itself must be carefully designed to avoid amplifying spurious high-frequency components [17].

Sustainability encompasses both environmental and computational dimensions. Training large deep learning models for hyperspectral unmixing consumes substantial energy, especially when hyperparameter optimization or ensembling is employed. The carbon footprint of such training campaigns is an increasingly acknowledged concern in the machine learning community, and remote sensing applications are not exempt [9]. Moreover, once deployed, models often need to be retrained or fine-tuned as new sensors become operational or as environmental conditions change over decadal timescales. Maintaining up-to-date training datasets that are representative of the evolving Earth system is a nontrivial infrastructure challenge. Endmember-aware architectures that can incorporate physical priors may reduce the need for frequent retraining, as the endmember representations are grounded in relatively stable material properties. However, the nonlinear interactions captured by the network may drift over time as land cover changes, necessitating periodic calibration.

## **6. Fairness, Governance, and Policy Implications**

Fairness considerations in hyperspectral unmixing are rarely discussed but are critically important given the socioeconomic and geopolitical contexts of Earth observation. Unmixing algorithms are used to estimate crop health, monitor pollution, assess mineral resources, and detect deforestation [2], [3]. Biases in training data—for instance, an overrepresentation of well-studied biomes such as temperate forests and underrepresentation of tropical savannas or Arctic tundra—can lead to systematically poorer performance in regions that are already underserved by scientific infrastructure. Endmember-aware feature learning, which relies on learning material signatures, may amplify these biases if the training set lacks diversity in spectral variability across different climates and terrains.

Governance of unmixing systems involves decisions about data access, model transparency, and accountability. Many hyperspectral datasets are proprietary or restricted due to national security concerns, which limits the ability of independent researchers to audit and validate unmixing models [10]. When endmember-aware models are deployed by government agencies or private companies for decision-making—such as in agricultural insurance, carbon credit verification, or military reconnaissance—the opacity of deep learning components raises concerns about explainability and redress. An endmember-aware architecture that produces interpretable intermediate representations could serve as a step toward algorithmic transparency, provided that the representations are accessible to domain experts and stakeholders.

Policy implications extend to international frameworks for sharing Earth observation data. The Global Earth Observation System of Systems and the Copernicus program emphasize open access, but the processing chains are often proprietary or vendor-locked [10]. Encouraging the adoption of standardized, open-source unmixing pipelines that incorporate endmember-aware learning could foster equity and reproducibility. However, such standardization must balance the need for flexibility to accommodate local environmental conditions with the desire for comparability across regions. Furthermore, the use of nonlinear unmixing models for resource extraction—for example, mapping rare earth elements from satellite data—raises questions about benefit-sharing and the potential for exacerbating resource conflicts. These governance dimensions require interdisciplinary collaboration among remote sensing scientists, ethicists, and policy makers.

## **7. Future Directions**

The evolution of endmember-aware feature learning for nonlinear hyperspectral unmixing is likely to be driven by several converging trends. First, the proliferation of hyperspectral sensors in small satellite constellations will generate massive data streams that demand automated and robust unmixing pipelines. Future architectures must be designed to operate in a federated learning setting, where models trained on one sensor can be rapidly adapted to another without full retraining. Endmember-aware representations that are sensor-invariant could facilitate such transfer learning [15], [18].

Second, the integration of physical models with data-driven learning—so-called physics-informed neural networks—offers a principled way to embed domain knowledge about radiative transfer into the unmixing framework. This can improve both consistency and generalization [4]. Combining endmember-aware feature learning with physics-informed loss functions that enforce energy conservation or scattering model constraints may reduce the need for large labeled datasets.

Third, fairness and accountability metrics need to be formally incorporated into the evaluation of unmixing systems. Benchmark datasets that are geographically and spectrally balanced, along with standardized reporting of performance across subgroups, would help identify and mitigate biases. Policymakers should consider mandating such reporting for any publicly funded Earth observation analysis.

Finally, the environmental impact of large-scale unmixing should be explicitly accounted for in system design. Energy-efficient neural architectures, such as spiking neural networks or lightweight transformers, could be explored for on-board processing, reducing the need to downlink massive volumes of raw data [9]. These developments align with broader sustainability goals in artificial intelligence.

## **8. Conclusion**

Endmember-aware feature learning represents a significant advancement in the field of nonlinear hyperspectral unmixing, offering the potential to improve both accuracy and interpretability by integrating domain knowledge about pure material signatures directly into deep learning pipelines. This paper has examined the system-level implications of adopting such frameworks, highlighting the architectural trade-offs between expressiveness, robustness, and scalability. We have argued that the deployment of endmember-aware models must consider not only algorithmic performance but also the broader context of infrastructure governance, computational sustainability, and fairness across diverse geographic and socioeconomic settings. The challenges of spectral variability, noise sensitivity, and data heterogeneity require careful regularization and adaptive mechanisms, while policy frameworks must evolve to ensure equitable access to high-quality Earth observation data and transparent algorithmic processes. Future research should focus on physics-informed integration, federated learning across sensor platforms, and the development of fairness-aware benchmarks. By adopting a holistic, interdisciplinary perspective, the remote sensing community can harness the power of endmember-aware feature learning while mitigating its risks and ensuring that the benefits of advanced unmixing are shared widely.

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